

Printing, folding and assembly methods for forming 3D mesostructures in advanced materials

Yihui Zhang¹, Fan Zhang¹, Zheng Yan², Qiang Ma¹, Xiuling Li³, Yonggang Huang⁴ and John A. Rogers⁵

Abstract | A rapidly expanding area of research in materials science involves the development of routes to complex 3D structures with feature sizes in the mesoscopic range (that is, between tens of nanometres and hundreds of micrometres). A goal is to establish methods for controlling the properties of materials systems and the function of devices constructed with them, not only through chemistry and morphology, but also through 3D architectures. The resulting systems, sometimes referred to as metamaterials, offer engineered behaviours with optical, thermal, acoustic, mechanical and electronic properties that do not occur in the natural world. Impressive advances in 3D printing techniques represent some of the most broadly recognized developments in this field, but recent successes with strategies based on concepts in origami, kirigami and deterministic assembly provide additional, unique options in 3D design and high-performance materials. In this Review, we highlight the latest progress and trends in methods for fabricating 3D mesostructures, beginning with the development of advanced material inks for nozzle-based approaches to 3D printing and new schemes for 3D optical patterning. In subsequent sections, we summarize more recent methods based on folding, rolling and mechanical assembly, including their application with materials such as designer hydrogels, monocrystalline inorganic semiconductors and graphene.

¹Center for Mechanics and Materials, AML, Department of Engineering Mechanics, Tsinghua University, Beijing 100084, China.

⁵Departments of Materials Science and Engineering, Biomedical Engineering, Neurological Surgery, Chemistry, Mechanical Engineering, Electrical Engineering and Computer Science; Center for Bio-Integrated Electronics; and Simpson Querrey Institute for BioNanotechnology, Northwestern University, Evanston, Illinois 60208, USA.

Correspondence to Y.Z. and J.A.R.

yihuzhang@tsinghua.edu.cn; jrogers@illinois.edu

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The development of strategies for forming 3D micro- and nanostructures in advanced materials is of increasing interest, driven by the potential for creating material systems with fundamentally new characteristics and functionalities. The notion of engineered materials, sometimes referred to as metamaterials^{1–5}, has its most prominent origins in electromagnetic structures with properties that do not occur naturally, such as negative refractive index⁴ and artificial magnetism². Here, extended 3D arrays of interconnected features with dimensions in the subwavelength regime allow exquisite control over the propagation of electromagnetic waves, with impressive examples in the microwave^{4,6–8}, terahertz^{9–11}, and infrared and visible^{12–16} regions of the electromagnetic spectrum. The required length scales span a wide range, from a few millimetres to tens of nanometres. The challenges in growth, assembly and/or fabrication are daunting, in which solutions require fundamental, conceptual advances in materials science and engineering. As examples, routes to 3D micro- and nanostructures for photonics include

colloidal self-assembly¹⁷, holographic lithography^{18–21}, direct-semiconductor or layer-by-layer growth^{22–25}, and two- or multiphoton lithography^{26–29}. Fabrication typically begins with formation of the necessary 3D architectures in materials optimized for this purpose, followed by exchange and/or templated growth to convert these materials into those required to yield desired optical responses. For example, two- or multiphoton lithography provides a means for patterning 3D structures with geometries suitable for photonic bandgap behaviour, but only in specialized, photosensitive materials that do not possess a sufficiently high dielectric constant. Therefore, these 3D structures are often used as templates for forming thin films of metals or semiconductors by atomic layer or chemical vapour deposition^{30–32}.

Modern use of the term ‘metamaterial’ spans materials that have structurally engineered behaviours in any property of interest, including optical^{12–16}, thermal^{33–35}, acoustic^{36–39}, mechanical^{40–48} and electromagnetic^{4,6–8}. Progress in nearly all cases relies critically on developments in materials and methods for forming 3D

Author addresses

¹Center for Mechanics and Materials, AML, Department of Engineering Mechanics, Tsinghua University, Beijing 100084, China.

²Department of Materials Science and Engineering and Frederick Seitz Materials Research Laboratory, University of Illinois at Urbana-Champaign, Urbana, Illinois 61801, USA.

³Department of Electrical and Computer Engineering, University of Illinois at Urbana-Champaign, Urbana, Illinois 61801, USA.

⁴Departments of Civil and Environmental Engineering, Mechanical Engineering, and Materials Science and Engineering, Northwestern University, Evanston, Illinois 60208, USA.

⁵Departments of Materials Science and Engineering, Biomedical Engineering, Neurological Surgery, Chemistry, Mechanical Engineering, Electrical Engineering and Computer Science; Center for Bio-Integrated Electronics; and Simpson Querrey Institute for BioNanotechnology, Northwestern University, Evanston, Illinois 60208, USA.

structures. For example, recent work demonstrates mechanical metamaterials^{40,42,43} in the form of ceramic and metallic micro- and nanolattices that reach previously inaccessible regimes of a parameter space defined by the strength, stiffness and weight. Advances in such types of mechanical metamaterials follow from the emergence of ingenious methods for multiphoton patterning and large-area projection micro-stereolithography (LAP μ SL)⁴⁴ that provide access to hierarchical structures with disparate 3D features with length scales from nanometres to centimetres. Lightweight metamaterials with tunable 3D negative thermal expansion can be achieved with carefully designed 3D periodic lattice units containing constituents with varied thermal expansion coefficients⁴⁹. This type of system can be realized with a multimaterial projection micro-stereolithography (P μ SL) method in which two distinct beam constituents join to form composite microlattices⁴⁹. Soft acoustic metamaterials can be formed with 3D structures that exhibit strong low-frequency Mie resonances^{50–52}. In certain examples, microfluidic strategies yield macroporous silicone microbeads randomly dispersed in gel matrices, with negative acoustic phase velocity over a broad range of frequencies⁵⁰.

3D micro- and nanostructures also offer powerful engineering design options for microsystem technologies, with relevance to biomedical devices^{53–57}, microelectromechanical systems (MEMS)^{58–60}, energy storage platforms^{61–66}, optoelectronic components^{67,68}, and others⁶⁹ (for example, electronics^{70–76}) where conventional, planar architectures currently dominate. As with metamaterials, progress follows from the ability to realize 3D structures in advanced materials. In addition to the optical techniques described previously, innovations in 3D printing techniques^{77,78} and associated inks^{70,79–86} based on metal, metal oxides, biomaterials and bio-compatible polymers represent notable recent developments. Alternative methods that exploit concepts in origami, kirigami^{87–92} and mechanically guided assembly^{74,75,93–97} provide complementary capabilities, with key advantages that derive from compatibility with modern planar technologies and associated thin-film deposition and processing techniques.

This Review highlights the latest results and future trends in these types of techniques (that is, printing,

folding, rolling and assembly) as routes to 3D mesostructures in advanced functional materials. The discussions begin with techniques for 3D printing that use scanning nozzles and patterns of light in schemes that utilize two-photon lithography (TPL) and P μ SL, including recent strategies that allow continuous, high-speed operation. Subsequent sections summarize methods based on folding and mechanical assembly, with application to materials such as designer hydrogels, monocrystalline inorganic semiconductors and graphene. We conclude by outlining some challenges and opportunities for future research.

Nozzle-based 3D printing technologies

The most widely used method for 3D printing relies on robotic control of scanning deposition nozzles in which 3D structures form in a layer-by-layer manner^{85,98–101}. Materials typically formulated from particulate and/or polymeric species with desired rheological behaviour serve as ‘inks’. Depending on the properties of the inks and the nature of the delivery process, these techniques can be further classified into two groups^{85,98,102}: inkjet printing for liquid inks and microextrusion printing for viscoelastic inks (FIG. 1a).

Inkjet printing, also known as drop-on-demand printing, exploits nozzles that use thermal or acoustic processes to deliver liquid droplets to desired locations on the substrate^{85,98,102–104}. By contrast, microextrusion printing uses pressure-induced flow to form continuous filaments of material, often designed to solidify immediately or shortly after emergence from the nozzle tip. In both cases, proper materials formulation is essential. For inkjet printing, the challenges are in realizing high solid content for thick deposits, but at sufficiently low viscosity to allow droplet generation in a manner that also avoids clogging of the nozzles¹⁰⁵. Although inkjet printing has widespread applications in forming 2D structures, 3D architectures can be difficult to form, partly owing to the uncontrolled flow of inks as they impinge on a structured surface¹⁰⁶.

By comparison, microextrusion printing offers far greater possibilities in 3D structuring owing to the broad range of ink designs and feature sizes. Microextrusion printers that offer modest (slightly sub-millimetre) resolution are now widely available in the form of commercial, user-friendly tools. In most cases, a printing head robotically controls the extrusion of a material ink onto a substrate, whereby a handling and dispensing system pneumatically or mechanically (with a piston or screw) controls the extrusion of materials in well-defined ambient conditions⁸⁵.

Recent research establishes methods for fabricating sophisticated 3D mesostructures with microscale resolution in a broad range of materials, including concentrated colloidal¹⁰⁷, nanoparticle¹⁰⁸, fugitive^{83,109} and polyelectrolyte¹¹⁰ inks. Main areas of current interest are in conductive and biomaterial inks because of their relevance in key applications, from solid-state lighting and wearable devices to tissue scaffolds and regenerative medicine. The following subsections highlight some of the latest progress.

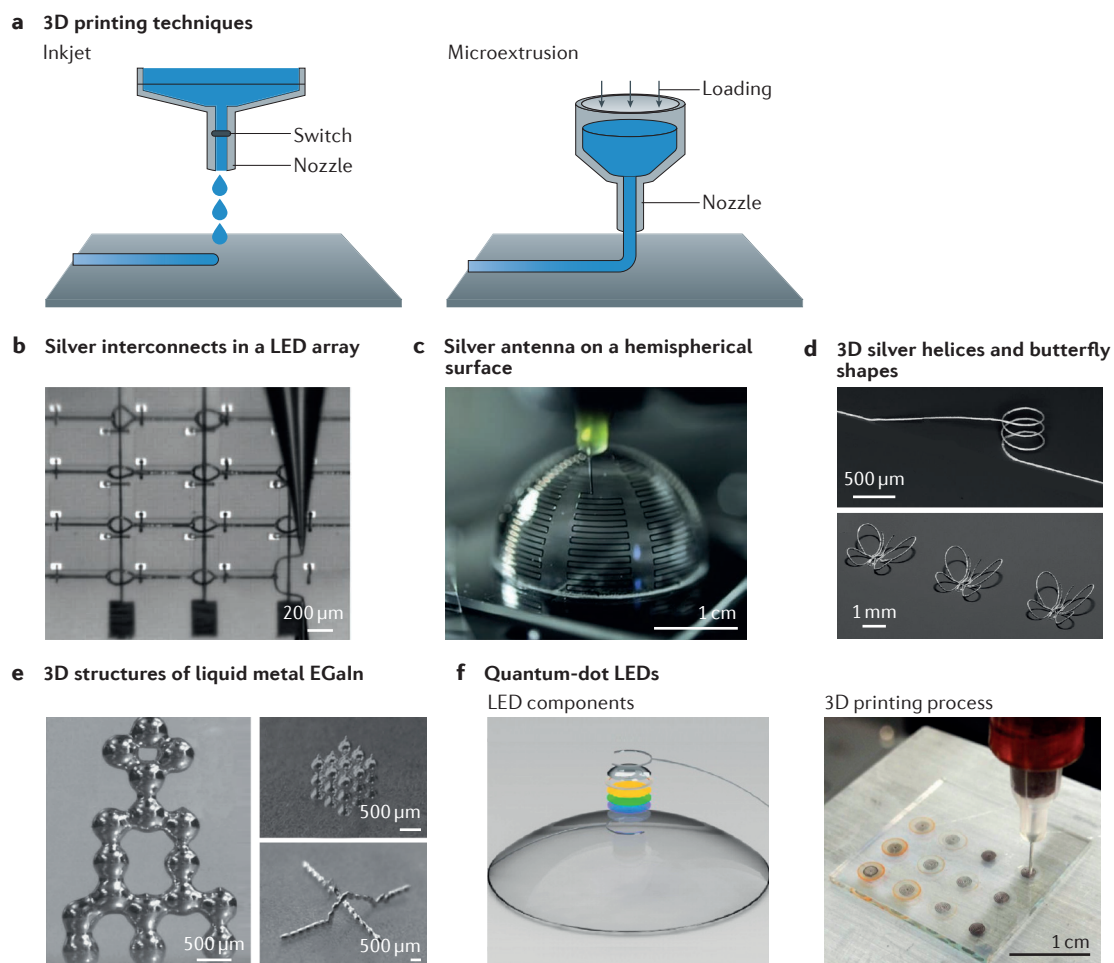


Figure 1 | Nozzle-based 3D printing technologies and applications in conductive structures. **a** | Schematic illustration of nozzle-based inkjet (left) and microextrusion (right) printing techniques. Inkjet printing usually relies on thermal or acoustic processes to deliver liquid droplets to desired locations on a substrate. Microextrusion printing uses pressure-induced flows to form continuous filaments of material, often designed to solidify immediately or shortly after emergence from the nozzle tip. **b** | 3D silver interconnects between an array of microscale light-emitting diodes (LEDs). **c** | A 3D silver antenna printed onto a hemispherical surface. **d** | 3D silver helices and butterfly shapes. **e** | 3D structures printed with the liquid metal EGaIn. **f** | Schematic illustration of quantum-dot LED components and an optical image acquired during 3D printing of this multimaterial structure. Panel **b** is adapted with permission from REF. 70, AAAS. Panel **c** is adapted with permission from REF. 79, Wiley-VCH. Panel **d** is adapted with permission from REF. 80, National Academy of Sciences. Panel **e** is adapted with permission from REF. 82, Wiley-VCH. Panel **f** is adapted with permission from REF. 84, American Chemical Society.

3D printing with conductive inks. One notable advance^{70,79,80} involves highly concentrated silver nanoparticle inks (>70 wt% Ag) for electrically conductive filaments in 3D arrangements (FIG. 1b,c). The viscoelastic properties enable self-supporting structures, such as the arc-shaped features in FIG. 1b. Thermal annealing (for example, at 150–500 °C) performed after printing by convective heating⁷⁰ or during printing by heating with a focused laser beam⁸⁰ can substantially improve the conductivity and the mechanical properties⁷⁰. As shown in FIG. 1d, 3D helical coils and butterfly shapes can be formed by heating during printing⁸⁰. Electrically functional devices, such as 3D spanning interconnects in arrays of microscale light-emitting diodes (FIG. 1b) and hemispherical antennas (FIG. 1c), suggest broad utility in electronics and optoelectronics^{70,79}.

Other strategies use liquid-metal inks in the form of binary eutectic alloys of gallium and indium (EGaIn)^{81–83}. EGaIn is a low-viscosity liquid at room temperature (with a melting point of ~15.7 °C). An ultrathin (~1 nm) passivating layer of gallium oxide forms immediately on exposure to air, thereby preventing spontaneous flow in ambient conditions⁸¹. As a result, at modest pressures (<5 kPa), metal filaments of EGaIn can be extruded to form free-standing structures. Additional options include the formation of 3D architectures of stacked droplets (FIG. 1e) delivered with a nozzle or of bars formed by the injection of metal into 3D microchannels created in sacrificial materials^{82,83}.

Sophisticated function in 3D structures typically demands the integration of several different types of materials, including, but not limited to, metals.

Achieving compatibility between different printed materials represents an additional challenge. In one successful example, a sequential printing process forms quantum-dot light-emitting diodes⁸⁴ (FIG. 1f) that incorporate five different materials, including emissive semiconductor nanoparticles, conductive polymers, solid or liquid metal leads, a transparent substrate and an elastomeric matrix, all in a 3D architecture. Another notable achievement is in multimaterial 3D printing of rechargeable lithium-ion microbatteries with high areal energy and power densities⁶⁶.

Despite these advances, existing methods in 3D printing cannot readily produce customized, fully integrated 3D electronic devices in a scalable manner. Opportunities exist in the development of advanced functional inks and flexible printing platforms (for example, multi-nozzle print heads) for rapid and precise patterning of materials over a broad range of compositions and ink-flow behaviours¹⁰⁵.

3D printing of biomaterials. Methods for 3D printing that are similar to those described above allow precise layer-by-layer positioning of biomaterials, living cells and/or biocompatible polymers into 3D structures with relevance to biology research and clinical medicine. As with applications in semiconductor devices, this type of bioprinting involves a complex interplay between geometry and material types, with the additional distinction that the resulting systems must accommodate time-dependent interactions with living systems, in which cell types, growth factors and dynamical mechanical and chemical effects can be critical⁸⁵. Nevertheless, recent advances enable the reproduction of certain key features of the complex microstructure of the extracellular matrix, including compatibility with multiple cell types and at sufficient resolution and fidelity to recapitulate biological function⁸⁵. For example, nozzles with diameters of 100–400 μm and inks of gelatin and fibrinogen that contain multiple cells and fugitive material of Pluronic F127 can be used to form thick (>1 cm and >10 cm³ in volume) artificial tissues with embedded vessels (<1 mm in diameter)¹¹¹. In a series of studies on synthetic heart valve conduits^{112–114}, biocompatible hybrid hydrogel inks patterned by 3D printing¹¹⁵ yielded tissue constructs with thicknesses of ~1 mm and diameters of ~2 cm. In other examples¹¹⁶, cartilage bodies with diameters and heights of 4 and 2 mm, respectively, result from inkjet printing with inks of poly(ethylene glycol) dimethacrylate and human chondrocytes, at layer thicknesses of 18 μm . Details of these efforts appear in other reviews^{85,102}. The main technological challenges are in increasing the resolution and manufacturing speed for clinically relevant sizes with a broadened set of biocompatible materials and an ability to maintain cellular viability and function. Additional opportunities exist in the heterogeneous integration of multiple biomaterials or of biomaterials with spatial gradients of compositions to achieve desired functional and mechanical properties. Printing of adaptive biomaterials with shapes, properties or functions that can be reprogrammed on demand represents an additional intriguing direction⁸⁵.

Two main areas of application are in synthetic tissues and organs for tissue engineering and for regeneration, with representative examples summarized in FIG. 2. An impressive range of synthetic tissues and organs can now be realized, including heart valve conduits^{112–114}, ear-shaped bionic structures¹¹⁷, tissue-engineered bones^{118–120}, vascular networks^{111,121} and certain components of the nervous system¹²². Bone scaffolds can be engineered with cellular microstructures that provide superior hyperelastic properties, including the ability to enable osteogenic differentiation of stem cells *in vivo* with or without osteo-inducing factors^{118–120}. Moreover, thick, heterogeneous cell-laden tissues can be perfused with printed vascular networks in a way that differentiates human mesenchymal stem cells towards an osteogenic lineage *in situ*^{111,121}. Another class of application relates to tissue regeneration and repair. Recent advances in skin and nerve regeneration^{123,124} and cartilage repair^{116,125} suggest great potential in these areas. For example, artificial, printed skin-like structures can be used for applications in wound closure, re-epithelialization and neovascularization of regenerating skin¹²³. Printed nerve scaffolds can be used in nerve regeneration following complex injuries, with the final pathway geometry adapted to the original tissue structure, in which physical and biochemical cues provide axonal guidance for bifurcating pathways¹²⁴.

Light-based 3D writing technologies

3D writing techniques that rely on patterned exposure of materials to light usually involve locally induced two- or multiphoton polymerization^{26,27,126–128}, UV photocuring^{129–131} or selective melting¹³². In contrast to nozzle-based methods, these techniques only operate effectively with a narrow range of materials, but they offer exceptionally high resolution and speeds of printing. This section focuses on three of the most promising techniques: TPL^{26,27,126–128}, PuSL^{43,44,131,133} and continuous liquid interface production^{77,78,134}, with highlights in applications for ultralight and ultrastiff mechanical metamaterials.

Two-photon lithography. In this approach, specially formulated photopolymers absorb two photons, typically in the infrared region of the spectrum, in a single quantum event, the collective energy of which corresponds to blue or near-UV light. As the rate of two-photon absorption is proportional to the square of the light intensity, absorption occurs preferentially at the waist of a highly focused laser beam, thereby confining the polymerization process to a volumetric region with sub-micrometre dimensions, often beyond the diffraction limit¹³⁵. A typical fabrication system consists of a collection of focusing lenses and beam-steering optics, a laser and a 3D scanning stage that supports a liquid bath of the photopolymer (FIG. 3a, left). As the focused laser beam scans laterally in the photopolymer and the stage scans vertically, the point of focus moves in a 3D trajectory under computer control, thereby enabling the fabrication of a desired 3D microstructure with ultrahigh resolution. Many schemes exist to improve the resolution (for example, to the sub-30 nm regime) and to expand the applicable material types, as summarized in other review articles^{29,135}.

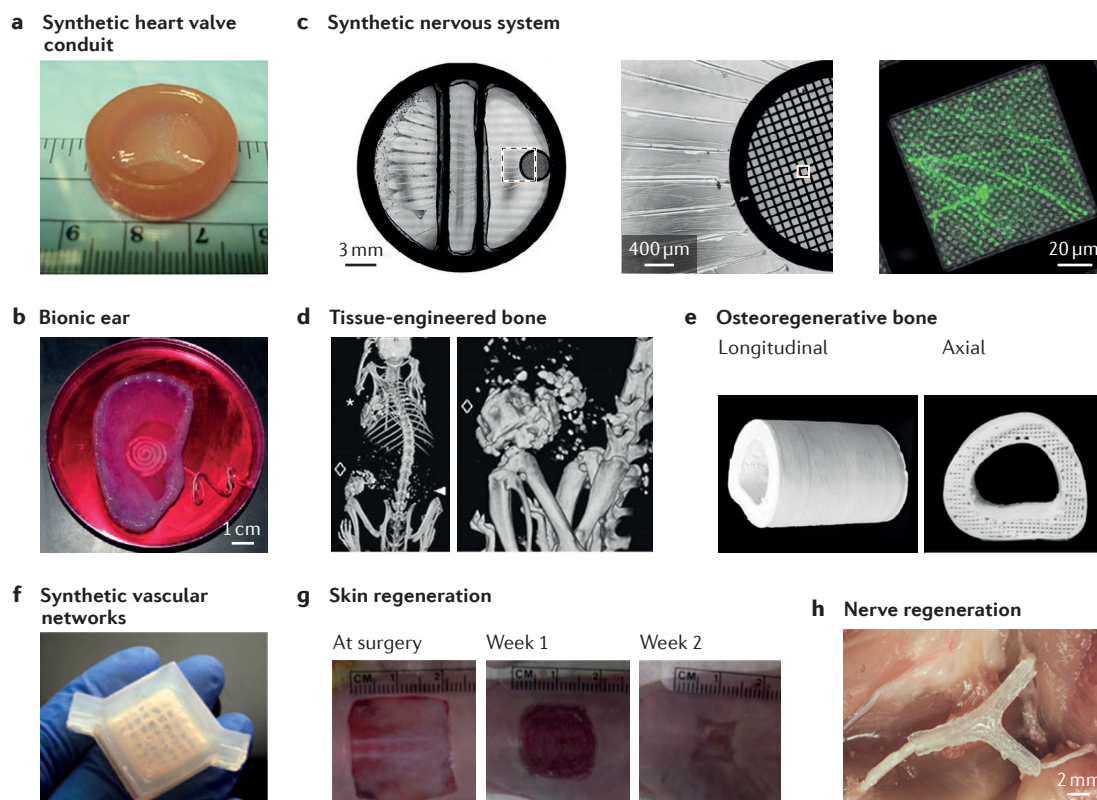


Figure 2 | Applications of nozzle-based 3D printing technologies in 3D bioprinting. **a** | Synthetic heart valve conduit. **b** | Bionic ear. **c** | Synthetic nervous system. **d** | Tissue-engineered bone. **e** | Osteoregenerative bone. **f** | Synthetic vascular networks. **g** | Skin regeneration. **h** | Nerve regeneration. Panel **a** is adapted with permission from REF. 113, Elsevier. Panel **b** is adapted with permission from REF. 117, American Chemical Society. Panel **c** is adapted with permission from REF. 122, Royal Society of Chemistry. Panel **d** is adapted with permission from REF. 118, Macmillan Publishers Limited. Panel **e** is adapted with permission from REF. 119, AAAS. Panel **f** is adapted with permission from REF. 111, National Academy of Sciences. Panel **g** is adapted with permission from REF. 123, AlphaMed Press. Panel **h** is adapted with permission from REF. 124, Wiley-VCH.

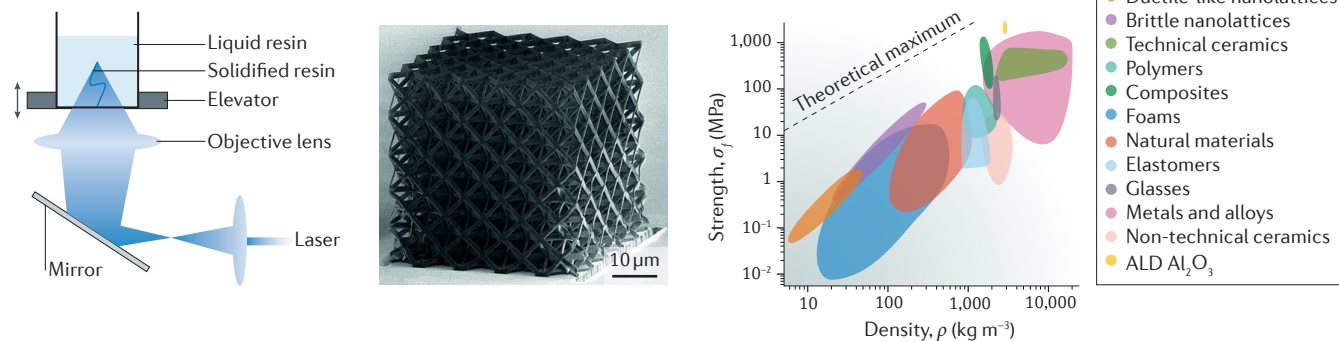
Owing partly to the remarkable spatial resolution that can be achieved, many advanced applications are possible in photonic metamaterials^{16,30–32,136–138}, MEMS and nanoelectromechanical systems (NEMS)^{139–142}, electronics^{143–146} and mechanical metamaterials^{41,42,147,148}. Mechanical metamaterials are of particular interest in the context of TPL because their mechanical properties can be defined not only by the geometries of the 3D architectures, but also by the ability to reduce the characteristic length scales (that is, several or tens of nanometres) to regimes in which size effects in material properties are pronounced.

To bypass materials constraints set by requirements for two-photon sensitivity, the 3D structures formed by TPL can serve as sacrificial templates for atomic-layer deposition, sputtering or plating of metals or ceramics to form nanolattices of these materials^{41,42,147–150}. The resulting systems have feature sizes that can extend to the nanoscale with, for example, wall widths and thickness in the ranges of 150–500 nm and 5–600 nm, respectively^{41,42,147,148,151,152}. Nanolattices of alumina are shown in FIG. 3a (middle), in which the hollow cross-sections of the constituent beams provide ultralight-weight construction⁴². Mechanical testing indicates that ceramic

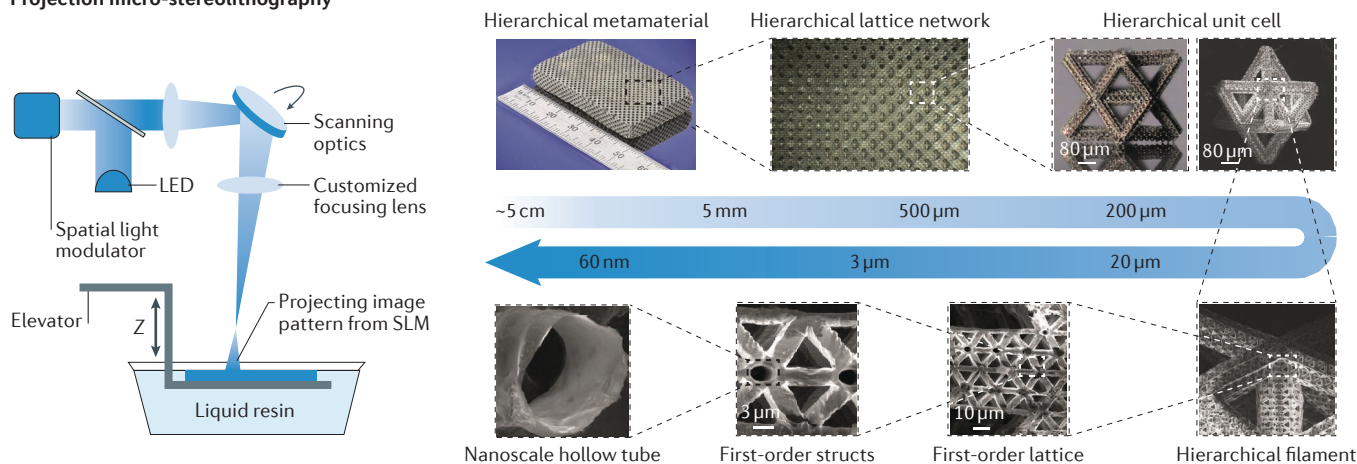
metamaterials of this type combine parameters of weight and strength (FIG. 3a, right) that are beyond those possible with the corresponding materials in unpatterned form. For example, such nanolattices have an ability to recover their original shape after compressive strains of 50% or more, owing to stretching-dominated deformations and elastic shell buckling in 3D architectures engineered for this purpose. Hierarchical metamaterials with fractal-inspired lattice layouts are also possible, as shown by recent studies of polymer, hollow ceramic and polymer–ceramic composites¹⁴⁷. Further developments are necessary, however, to increase the patterning speeds and scalability (that is, manufacturing a large number of small-scale components in a reasonable time) needed for practical applications.

Projection micro-stereolithography. As in traditional stereolithography, PμSL forms complex 3D mesostructures in a layer-by-layer manner based on photopolymerization reactions in resin materials^{43,131,133}. Each layer corresponds to a 2D image of a sectional slice of a desired 3D shape, formed by projection through a spatial light modulator using a demagnifying lens system. Exposure to UV light solidifies the liquid resin to

a Two-photon polymerization



b Projection micro-stereolithography



c Continuous liquid interface production

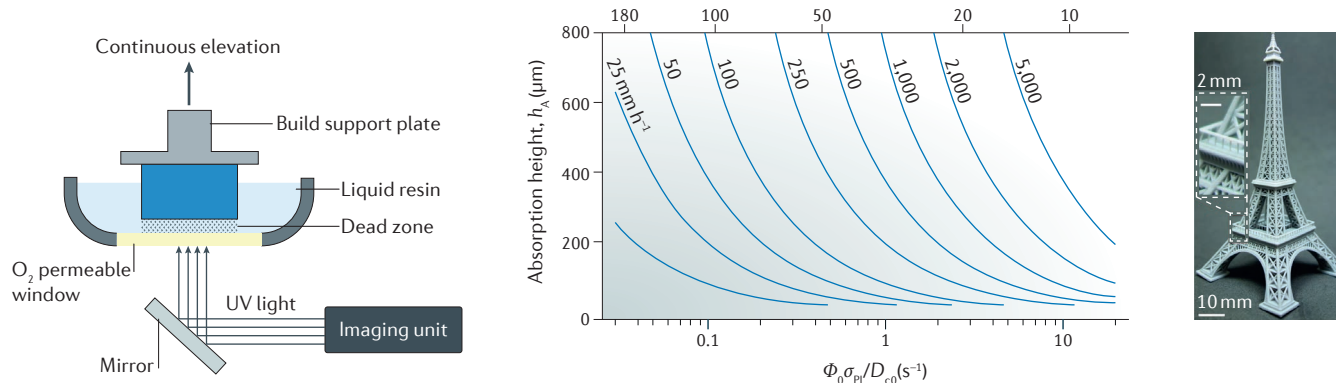


Figure 3 | Light-based 3D printing technologies: schemes, structures and properties. **a** | Multiphoton polymerization: schematic illustration in which a highly focused laser beam polymerizes photopolymers by two-photon effects in volumetric regions with sub-micrometre dimensions (left). Scanning electron micrographs of an alumina octet-truss nanolattice (middle). Strength as a function of density for various materials (right). **b** | Large-area projection micro-stereolithography (LAPμSL): schematic illustration in which a portion of a 2D image (corresponding to a sectional slice of a desired 3D shape) is formed by projection through a spatial light modulator (SLM), and then directed dynamically through an optical scanning system onto a corresponding region of the resin to solidify the entire 2D layer of the liquid resin (left). Optical microscope images and scanning electron micrographs of a hierarchical 3D metamaterial fabricated by LAPμSL, with a cross-sectional highlight of its structural hierarchy (right). **c** | Continuous liquid interface production (CLIP): schematic illustration in which an oxygen-permeable window creates a narrow, oxygen-inhibited zone to locally prevent photopolymerization, thereby allowing for simultaneous UV exposure, resin renewal and elevation of the build support plate (left). CLIP print speed as a function of the characteristic optical absorption height and the combined parameter $\Phi_0 \alpha_{PI} / D_{c0}$ (middle). Eiffel Tower model printed using CLIP (right). Panel **a** (middle and right) is adapted with permission from REF. 42, AAAS. Panel **b** is adapted with permission from REF. 44, Macmillan Publishers Limited. Panel **c** is adapted with permission from REF. 78, AAAS.

form a thin, solid 2D layer in the geometry of the image. Lowering the substrate, coating the pattern with uncured resin and then repeating the process eventually completes the 3D fabrication. This scheme provides excellent structural diversity, with resolution in the micrometre range over areas of several centimetres⁴³, comparable to that achieved with a photopolymer waveguide technique⁴⁰. The parallel operation enables speeds that are much higher than those of serial approaches such as TPL and nozzle-based printing. However, traditional methods have limited fields of view and associated difficulties in forming hierarchical geometries with diverse feature sizes over large areas.

A recent variant — large-area projection micro-stereolithography (LAP μ SL)⁴⁴ — overcomes these disadvantages through the use of an optical scanning system that dynamically directs a portion of the 2D image onto a corresponding region of the resin in a coordinated, sequential manner to complete the entire 2D layer (FIG. 3b, left). The power of LAP μ SL is demonstrated by the formation of metallic hierarchical lattices with different structural topologies, for which the minimum feature size (50 nm) is several orders of magnitude smaller than the overall size of the sample (~5 cm)⁴⁴ (FIG. 3b, right). An alternative approach combines P μ SL with methods based on folding or mechanically guided assembly in an integrated approach to allow for rapid formation of hierarchical lattices or other 3D architectures with diverse feature sizes.

Continuous liquid interface production. Dramatic improvements in micro-stereolithography follow from ideas that eliminate the need to coat the resin after each exposure. The key concept involves an oxygen-permeable window that creates a narrow, oxygen-inhibited zone to locally prevent photopolymerization, and an exposure system that illuminates the resin bath through this window from beneath^{77,78} (FIG. 3c, left). Specifically, this setup incorporates a thin, uncured liquid layer (that is, a dead zone) between the window and the photopolymerized resin, where oxygen quenches the photoexcited photoinitiator. This lubricating film allows for simultaneous UV exposure, resin renewal and platform (that is, a build support plate) movement in the upward direction, thereby avoiding the separate, discrete steps required in traditional micro-stereolithography. The resulting process, known as continuous liquid interface production, offers throughputs that are much higher than those previously possible, typically by more than an order of magnitude^{77,78}. The thickness of the dead zone depends on the incident photon flux (Φ_0), the photoinitiator absorption coefficient (α_{pi}) and the curing dosage (D_{c0}), according to $(\Phi_0\alpha_{pi}/D_{c0})^{-0.5}$ (REF. 78). As a consequence, the print speed approximately scales with the combined parameter $(\Phi_0\alpha_{pi}/D_{c0})$ and the absorption height (that is, the resolution) of the resin for geometries in which the speed-limiting process is resin curing (FIG. 3c, middle). For target geometries with comparatively wide solid cross-sections, these predictions of print speed do not apply, because the flow of resin into the building area becomes a dominant consideration. Complex 3D

mesostructures, for example, the Eiffel Tower in FIG. 3c (right), can be drawn out of a resin bath at rates of hundreds of millimetres per hour. This rate of production has some potential for use in high-volume manufacturing of delicate microscale parts, such as microneedles for transcutaneous drug delivery¹³⁴.

Stress-controlled folding of 3D systems

A set of strategies that complement the direct fabrication routes described previously exploits stress-controlled folding and/or mechanically guided assembly of 2D precursor structures. Such schemes fully leverage the sophisticated technologies that exist for micro- and nanofabrication, and for materials deposition in the semiconductor and integrated photonic industries, ranging from patterning methods (for example, projection-mode photolithography) to processing techniques (for example, etching and thin-film deposition) and material growth strategies (for example, epitaxial growth and doping). This section focuses on methods for folding induced by internal stresses, including two classes of advanced techniques based on 4D printing and micro- and nanoscale origami. A subsequent section reviews strategies of mechanically guided, deterministic assembly via forces imposed by a supporting substrate.

4D printing. In this scheme, 3D printing techniques form structures that have a bilayer or multilayer heterogeneous design with mismatched strains that follow from external stimulation — for example, exposure to water or heat — thereby inducing self-folding or self-rolling into 3D shapes that are responsive to their environment and/or would be difficult to print directly. Representative material systems include hydrogels^{153–155} and shape-memory polymers (SMPs)^{156–158}.

One example of hydrogel-based 4D printing uses a composite ink in programmable bilayer architectures¹⁵³, wherein the constituent filaments exhibit anisotropic stiffness and swelling behaviour (FIG. 4a). Differential swelling between the top layer and bottom layer leads to controlled folding deformations and spatially varying curvatures that depend mainly on the elastic moduli, the swelling ratios, the thickness ratio of two different layers and the total bilayer thickness. Quantitative mechanics models that extend the classical Timoshenko theory for bimetallic strips can capture all of these effects, allowing predictions of the final, fully hydrated state. Reversible changes in 3D configuration are possible with stimuli-responsive (for example, temperature) hydrogels¹⁵³. The hydrogel can also be laminated against a passive polymeric material to form a self-evolving joint capable of folding, curling, twisting, and linear expansion or shrinkage, on exposure to water^{154,155}.

In SMP-based 4D printing¹⁵⁶, 3D-printed bilayer structures comprise a matrix and a laminate with embedded SMP fibres (FIG. 4a). Controlled 3D transformation can be achieved by stretching at temperatures above the characteristic transition of the SMP, followed by cooling and releasing the externally applied force. Impressive examples of dynamically changing 3D structures can be achieved with different material systems (FIG. 4b), such as

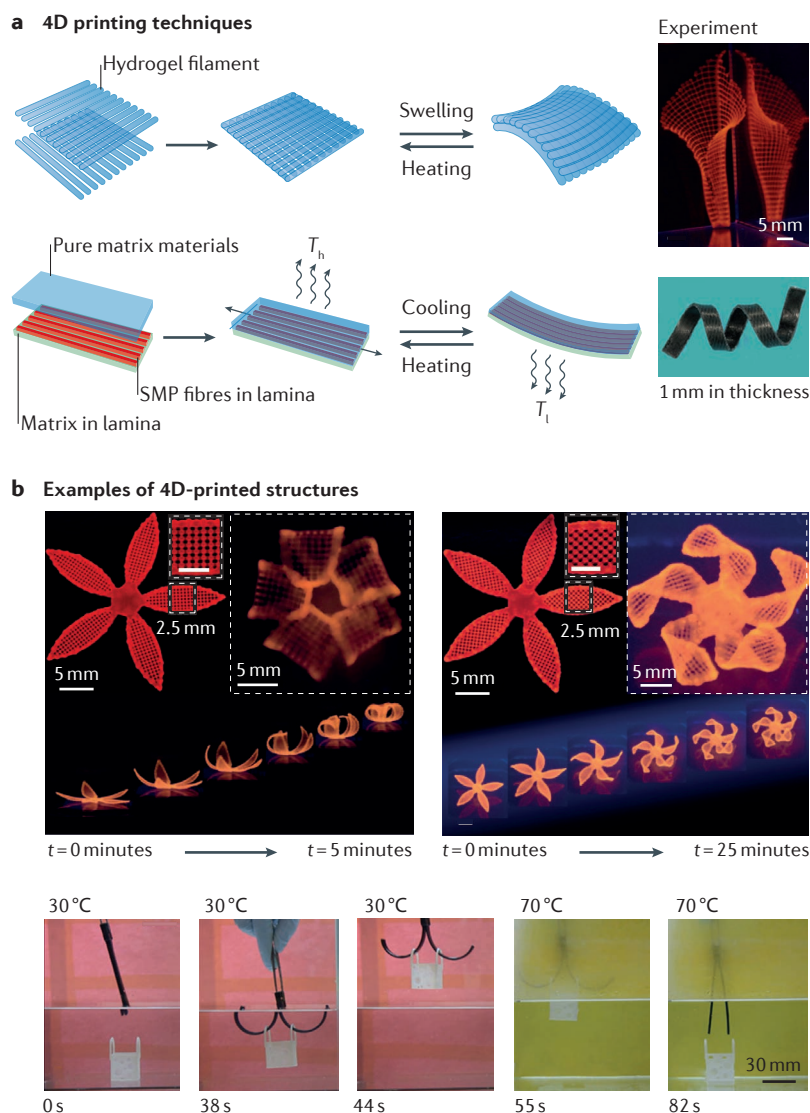


Figure 4 | 4D printing schemes and time-evolving structure geometries. **a** | Schematic illustration of two 4D printing techniques and images of representative structures. The schematic illustration on the top shows a 3D-printed hydrogel bilayer composite, in which differential swelling between the top layer and bottom layer induces controlled folding deformations, leading to time-evolving 3D transformation from the original 2D shape. The schematic illustration on the bottom shows a 3D-printed bilayer structure of a matrix and a laminate with embedded shape-memory polymer (SMP) fibres, which can achieve controlled 3D transformation through the action of strain in the SMP developed by changes in temperature across the glass transition point (T_g). **b** | Two hydrogel patterns with flower geometries and different petal patterns, with time-lapse images that illustrate the geometrical transformation induced by swelling (top). Application of SMP-based 4D printing to form a programmable hook, in which a small box is lifted up from a container immersed in water at 30 °C, and then released into another water-filled container at 70 °C (bottom). T_h , a temperature higher than T_g ; T_l , a temperature lower than T_g . Panel **a** is adapted with permission from REF. 153, Macmillan Publishers Limited, and REF. 156, AIP Publishing. Panel **b** (top) is adapted with permission from REF. 153, Macmillan Publishers Limited. Panel **b** (bottom) is adapted with permission from REF. 158, Macmillan Publishers Limited.

a programmable hook that can grasp objects and then release them using a thermal switching mechanism. An intriguing future direction is in the development of new printable materials that can respond to external stimuli at desired rates.

Micro- and nanoscale origami. Folding deformations can serve as the basis for origami-inspired assembly at micro- or nanoscales^{69,159–162}. In most published examples, the necessary forces arise from capillarity, thin-film residual stresses or mechanically active (that is, stimuli responsive) materials. As an example of capillary forces^{163–168}, heating a solder above its melting point drives the folding of adjacent panels as the solder reconfigures its shape to minimize the surface energy (FIG. 5a, left). Water droplets can also provide sufficient capillary forces for this type of origami assembly^{89,90}. Various classes of closed-form polyhedral mesostructures can be realized in this manner^{89,167,168}, with representative examples in FIG. 5b.

Schemes based on thin-film residual stresses typically rely on strain mismatch between different materials in a multilayer stack to induce self-rolling upon removal of an underlying sacrificial layer^{169–172}. A schematic illustration of this strategy is shown in FIG. 5a (middle), in which a strain gradient along the thickness direction can be controlled through relevant parameters (for example, temperature, frequency, composition and deposition rates) associated with the thin-film deposition process. This strategy can produce mesostructures with tubular, scroll-like or polyhedral geometries, in a range of material systems (for example, Pt, ZnO, Al₂O₃, Si_xN_y, TiO₂, SiGe, Si_xN_y-Ag, InGaAs-GaAs and Pd-Fe-Pd)^{71–73,91,169,170,173–180}. Examples of tubes achieved in this way are shown in FIG. 5c.

Another strategy involves active materials (for example, hydrogels^{181–186}, SMPs or shape-memory alloys (SMAs)^{187–189}, liquid crystal elastomers^{190,191} or photoactive polymers^{192,193}) to create spatially non-uniform strains, either along the in-plane or out-of-plane (that is, thickness) directions, thereby deforming planar structures into desired 3D shapes. A schematic illustration appears in FIG. 5a (right), in which a multilayer hydrogel design provides a folding mechanism similar to that based on thin-film residual stresses. This scheme offers a high degree of flexibility in hierarchical 3D design (FIG. 5d). In the examples of FIG. 5b–d, the final 3D configuration typically represents a state of equilibrium that results from minimization of the total system energy, which consists of the strain energy (in terms of bending energy and membrane energy for various layers within the thin films) and the work done by an external force (for example, capillary forces). This total energy can be expressed as functions of local curvatures according to mechanics models, which then define relationships between the various driving forces, the geometric parameters and the curvature of the target surfaces.

Compatibility of strategies based on capillary forces and thin-film residual stresses with established planar technologies suggests potential for building new classes of 3D electronic, optoelectronic and biomedical devices. Examples include solar cells with improved efficiency in light harvesting⁹⁰, cell grippers capable of separating and isolating single cells¹⁷⁸, antennas that allow implantation using standard medical syringes¹⁷⁵, and inductors for radio-frequency-integrated circuits with extremely small form factors and improved electrical performance, particularly at frequencies for 5G wireless communication

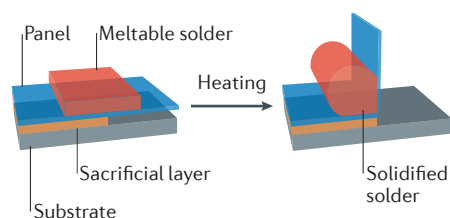
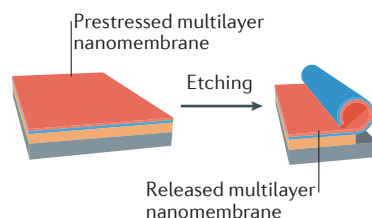
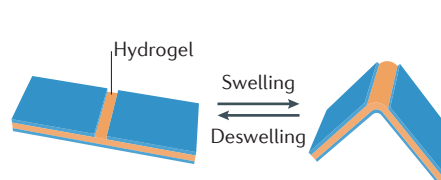
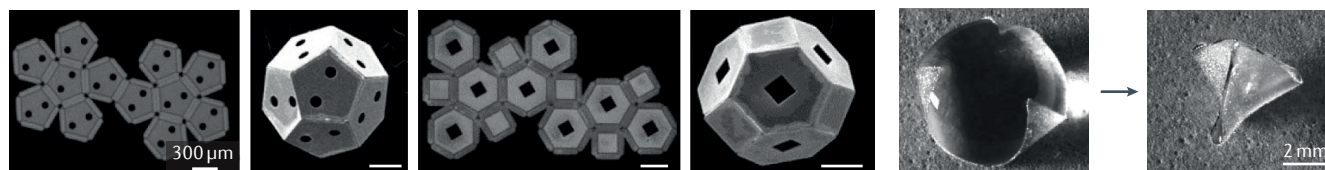
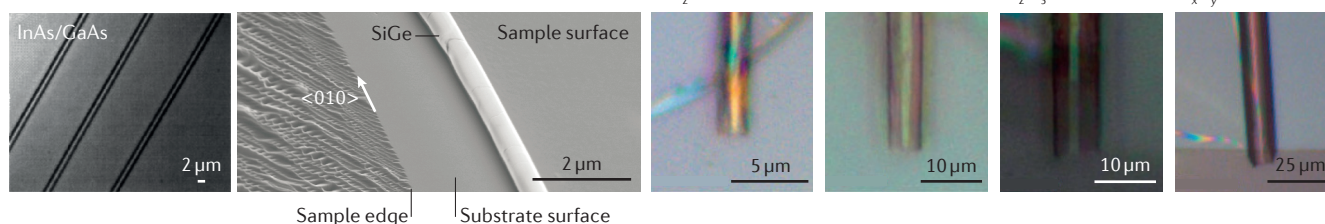
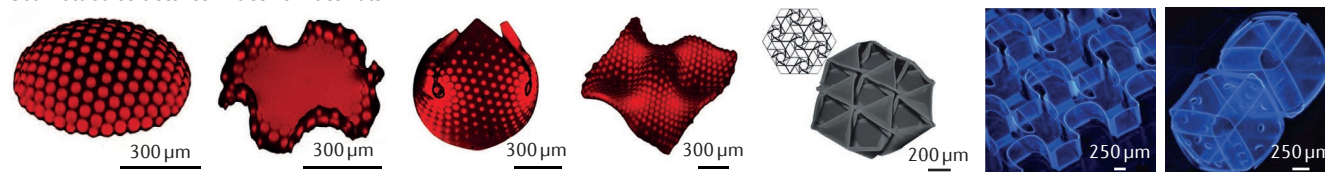
a Mechanisms of folding deformation**Capillary forces****Thin-film residual stresses****Active materials****b SEM images of folded structures****c Residual stress-induced self-folded and rolled structures****d Self-folded structures in active materials**

Figure 5 | Micro- and nanoscale origami: schemes, structures and device applications. **a** | Schematic illustrations of methods that rely on capillary forces (left), thin-film residual stress (middle) and active materials (right). **b** | Optical and scanning electron microscope (SEM) images of folded structures formed using capillary forces, including a dodecahedron and an octahedron of nickel, and a tetrahedron of polydimethylsiloxane. **c** | Optical and SEM images of residual-stress induced self-folded or rolled structures in a range of materials. **d** | Self-folded structures in active materials: hydrogels (left five images) and photopatterned polymers (right two images). Panel **b** (four images, left) is adapted with permission from REF. 168, National Academy of Sciences. Panel **b** (two images, right) is adapted with permission from REF. 89, American Physical Society. Panel **c** is adapted with permission from REF. 169, Elsevier; REF. 170, Macmillan Publishers Limited; and REF. 176, Wiley-VCH. Panel **d** is adapted with permission from REF. 182, AAAS; REF. 183, Wiley-VCH; and REF. 192, Macmillan Publishers Limited.

and beyond^{76,194}. Remaining challenges are in achieving reversible and programmable self-folding of high-performance materials at micro- or nanoscale. Opportunities exist in the development of techniques for the micro- and nanoscale patterning of 2D thin films of active materials (for example, SMP or SMA) and their heterogeneous integration with passive layers of high-performance, electronic materials.

Recent studies explore the fundamental limits of this type of process, using graphene as either the structural material or the material at the primary locations of bending^{92,195}. The atomic-scale thickness of graphene leads to the possibility for exceptionally small radii of curvature. Graphene with kirigami-inspired patterns and lateral feature sizes of $\sim 2\ \mu\text{m}$ can be assembled into 3D

configurations under in-plane or out-of-plane loading⁹² (FIG. 6a,b). In these examples, mechanical stages, magnetic forces or other externally imposed stimuli drive the assembly. Self-tearing or peeling of graphene from a substrate by thermal activation can also lead to folding deformations¹⁹⁵, thereby providing a route to origami processes (FIG. 6c). Atomistic simulations provide insights into the underlying physics^{196–201}.

Mechanically guided assembly

The techniques described above apply most readily to plates or simple curved structures (for example, tubes and scrolls), where the most sophisticated 3D geometries consist of closed- or open-form polyhedra and their variants, or cylindrical structures. Recently introduced approaches

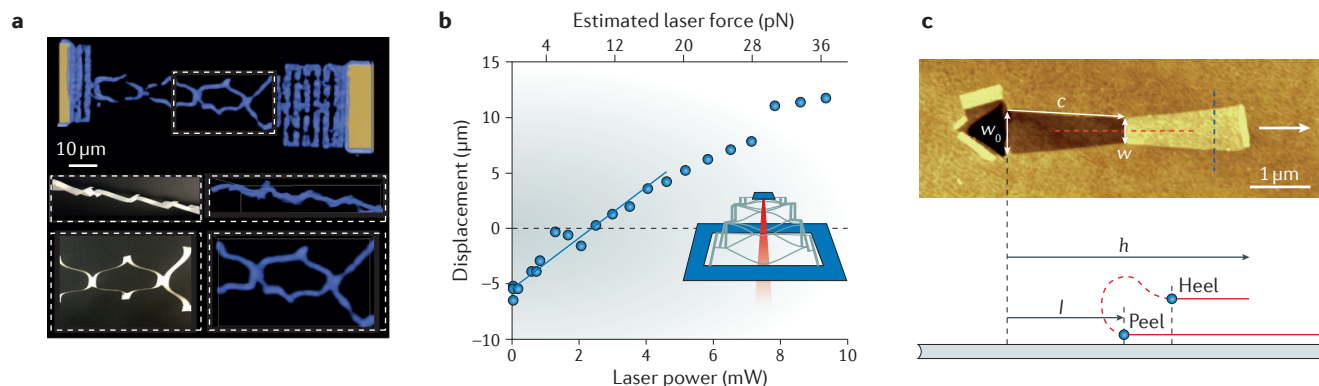


Figure 6 | Graphene origami and kirigami. **a** | 3D reconstruction from a z-scan focal series of images of a spring made from graphene with a lithographically defined pattern of cuts, with insets that show side and top views of sections of the graphene (right) and corresponding paper models (left). **b** | Measurements of displacement as a function of laser force for a graphene pyramid, with a schematic shown in the inset. **c** | Atomic force microscopy image of a folded graphene ribbon and schematic illustration of a side view of the ribbon, featuring the fold cross-section with excess length $\zeta = 2l - h$ (dashed red curve between surface peel and heel points, indicated by blue dots). c , path length of the two tears (assumed to be identical) that define the ribbon shape; w_0 , nucleation fold width; w , final fold width. Panels **a** and **b** are adapted with permission from REF. 92, Macmillan Publishers Limited. Panel **c** is adapted with permission from REF. 195, Macmillan Publishers Limited.

based on mechanically guided assembly involve precisely controlled, deterministic 2D–3D transformations⁷⁴ that expand the range of accessible 3D geometries, while maintaining compatibility not only with the methods described in the previous sections, but also with 2D microsystems technologies.

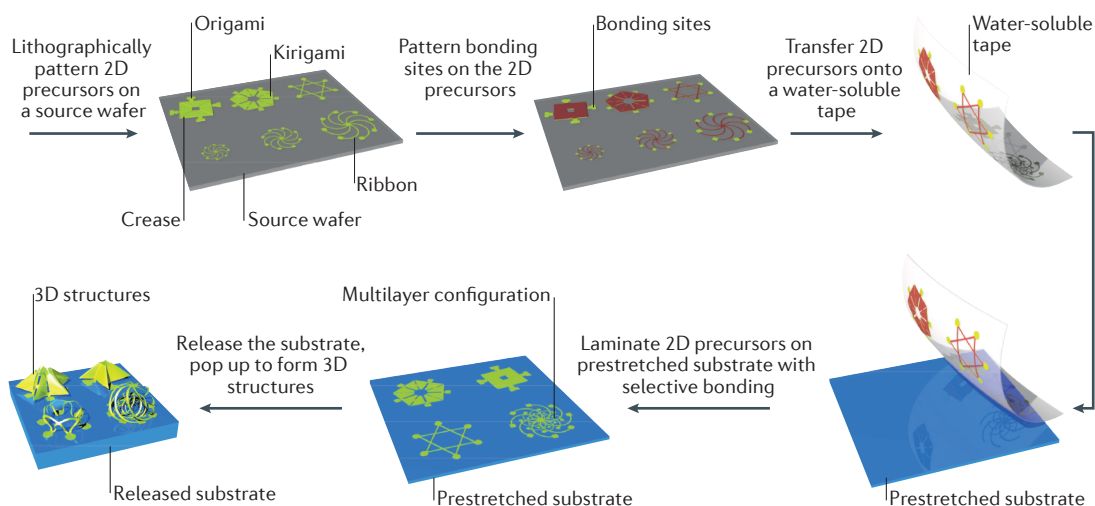
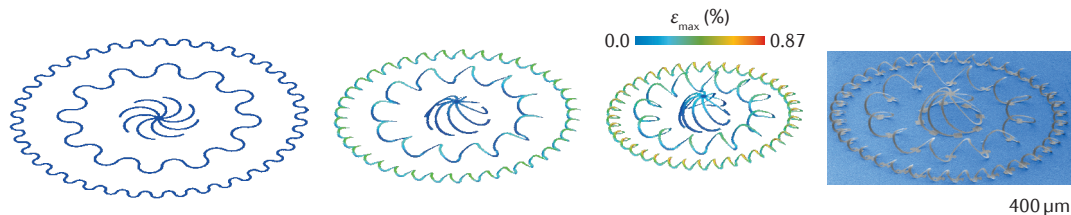
This process begins with the formation of a thin 2D precursor on a source wafer or other planar substrate, followed by the release and then precise patterning of regions that establish strong sites of adhesion to a pre-stretched elastomeric substrate (that is, an assembly platform) upon contact^{74,75,93,95} (FIG. 7a). Release of the prestretch induces compressive forces at the bonding sites. The result causes the 2D precursor to geometrically transform, through spatially dependent deformations and in- and out-of-plane translational and rotational motions, into an engineered 3D configuration. The effect provides access to wide-ranging classes of topologies, for which the key control variables include: the 2D layout, thicknesses and mechanical properties of the precursor structures; the pattern of sites for selective bonding; and the nature and magnitude of the prestrain in the assembly platform.

Quantitative mechanics modelling can capture all of these factors at a precise quantitative level across 3D configurations with a rich diversity of complex shapes^{74,75,93–95}. As an example, an elaborate 3D mesostructure formed of ribbons of device-grade, monocrystalline silicon is shown in FIG. 7b. The layout consists of a concentric pair of toroids and a separate hemispherical ‘cage’ construct at the centre. Guided by mechanics modelling, a wide range of filamentary mesostructures are possible⁷⁴, from helices, toroids and conical spirals, to structures that resemble spherical baskets, cuboid cages, starbursts, flowers, scaffolds and frameworks, each with single- and/or multiple-level configurations (FIG. 7c).

A broadened range of options follows from kirigami- or origami-inspired designs in the precursors^{93,95,96}.

For example, engineered variations of thickness in the 2D precursors can guide folding deformations at specific, targeted locations, owing to the cubic dependence of the bending stiffness on thickness. 3D mesostructures composed of membranes, plates, ribbons and wires, with continuously curved shapes and/or sharp folds between flat constitutive elements, can be achieved (FIG. 7d,e). The use of releasable, multilayer 2D precursors allows dense 3D architectures (FIG. 7f) with nested layouts, controlled points of entanglement and other features that are unobtainable with single-layer 2D precursors⁷⁵. In addition, the elastomeric substrate itself can be engineered to achieve non-uniform distributions of strain in the pre-stretched state. The result provides desired strain fields for complex but well-defined control over the resultant 3D geometries⁹⁷.

An appealing feature of this scheme is that it has immediate, broad applicability to nearly any type of material, including inorganic semiconductors, metals, polymers and various heterogeneous combinations, spanning length scales from sub-micrometre to metre dimensions. FIGURE 8a highlights two 3D structures with length scales that range from sub-micrometre, to micrometre, millimetre, centimetre and metre dimensions²⁰². The use of a diverse collection of materials (for example, Ni, Au, epoxy (SU8), polyimide, SU8–Au and SU8–Si) is also possible (FIG. 8b). Compatibility with state-of-the-art 2D fabrication, processing and growth techniques allows the transformation of virtually any type of existing 2D microsystem technology into a 3D configuration, thereby providing unusual design options and unique devices. Examples range from mechanically tunable spiral micro-inductors⁷⁴, the quality factor and resonance frequency of which can be adjusted in a reversible manner through deformations of the elastomer substrate (FIG. 8c), to near-field communication devices⁷⁵ that offer improved enhanced quality factor and expanded working angles compared with those of conventional 2D

a Mechanically guided assembly of 3D mesostructures

b Finite-element analysis and SEM image of a complex silicon mesostructure

c Filamentary silicon mesostructures

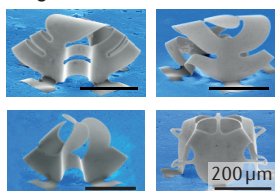
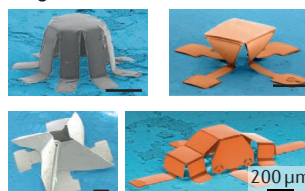
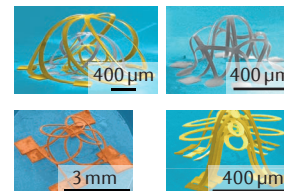
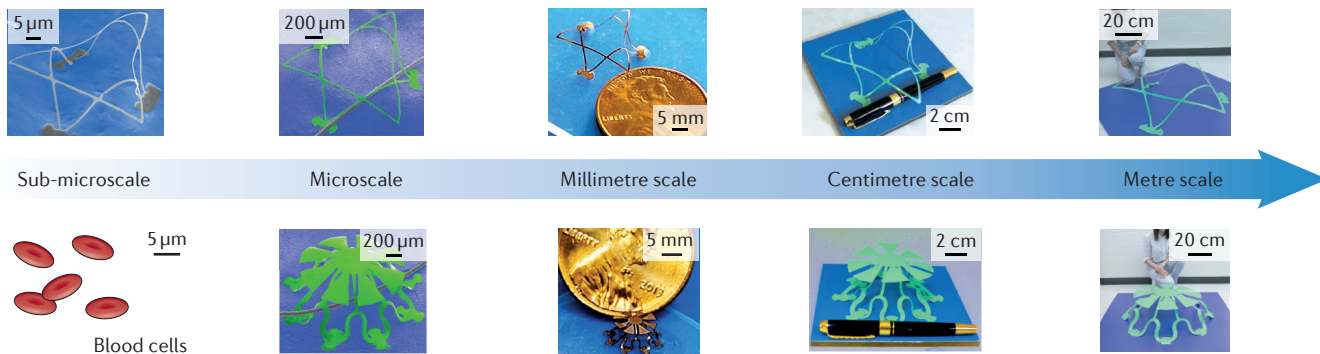
d Kirigami mesostructures

e Origami mesostructures

f Multilayer mesostructures


Figure 7 | Mechanically guided self-assembly: schemes and structures. **a** | Schematic illustration of steps for fabricating 3D mesostructures by controlled mechanical buckling of 2D precursors formed using lithographic techniques. **b** | Finite-element analysis results (left three frames) that describe the 2D to 3D geometrical transformation associated with the formation of a complex 3D silicon mesostructure that consists of a concentric pair of toroids and a separate hemispherical 'cage' at the centre, along with a corresponding scanning electron microscope (SEM) image (right) of the final configuration. **c** | Optical images of various 3D filamentary silicon mesostructures. **d** | SEM images of various 3D kirigami mesostructures of silicon and epoxy bilayers. **e** | SEM images of various 3D origami mesostructures with different materials (silicon coloured in grey and metals coloured in orange). **f** | SEM images of various 3D multilayer mesostructures with different materials (epoxy coloured in yellow, silicon coloured in grey and metals coloured in orange). ϵ_{\max} , maximum principal strain. Panels **b** and **c** are adapted with permission from REF. 74, AAAS. Panel **d** is adapted with permission from REF. 93, National Academy of Sciences. Panel **e** is adapted with permission from REF. 95, Wiley-VCH. Panel **f** is adapted with permission from REF. 75, AAAS.

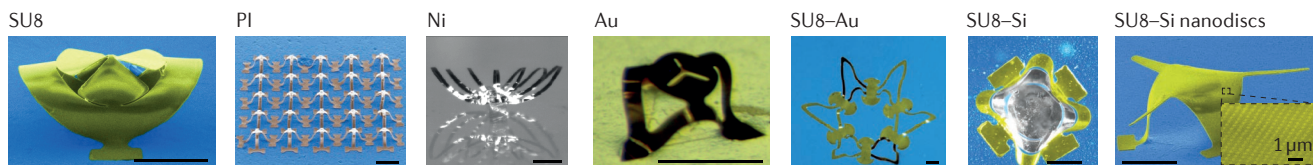
counterparts (FIG. 8d). Rotating micro-mirrors with tilt angles that can be adjusted in a programmable manner for beam steering and modulating the transmission are also possible⁹³. The use of active or passive cell scaffolds as 3D frameworks represents an additional area of active exploration.

Further advances will follow from the development of routes to free-standing, isolated 3D mesostructures after separation from the elastomeric substrates. Opportunities also exist in extending these concepts in mechanical assembly from structures with lateral sizes in the nano-scale regime to graphene and other 2D materials.

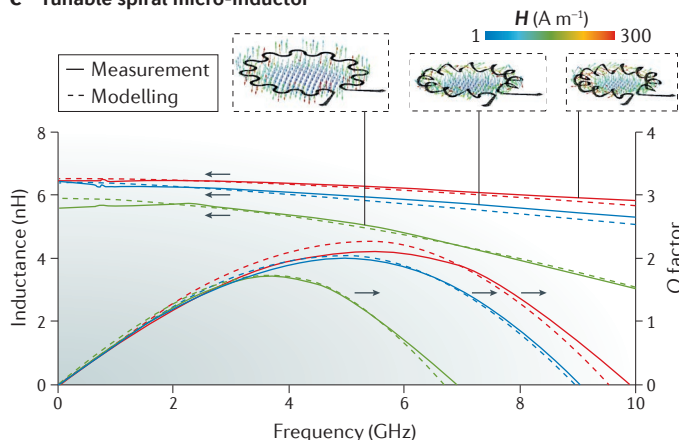
a Starfish- and jellyfish-like structures



b 3D mesostructures of different materials



c Tunable spiral micro-inductor



d Near-field communications device

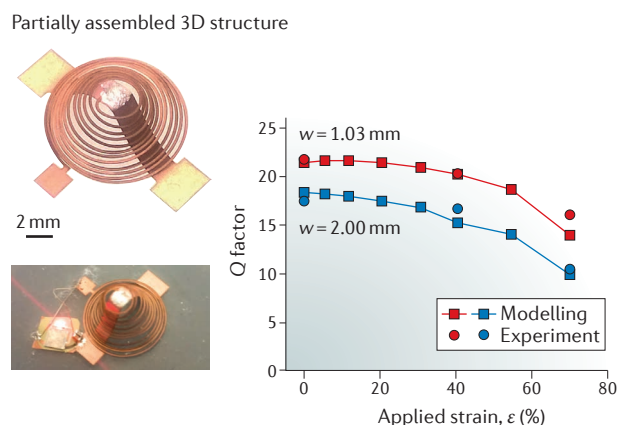


Figure 8 | Mechanically guided self-assembly: material and size diversity with applications. **a** | 3D starfish-like and jellyfish-like structures with characteristic dimensions that span a wide range of length scales. The materials for the sub-micrometre, micrometre, millimetre, centimetre and metre scale structures are silicon, polyimide, bilayers of copper and polyimide, polyester and polyvinyl chloride, respectively. **b** | Experimental images of 3D mesostructures made of metal (Ni and Au), polymer (epoxy (SU8) and polyimide (PI)), and heterogeneous combinations of these materials (SU8–Au and SU8–Si). Scale bars are 200 μm. **c** | Frequency dependence of the inductance and the Q factor of a circular inductor mechanically configured into three different shapes. The images are simulation results for the magnetic field (H) distributions (feed-in power, 1 W), in which the arrows indicate the direction and their colours indicate the magnitude. **d** | Optical images of a 3D near-field communication device at partial and full release of prestretch in the substrate, and during power supply to a red light-emitting diode. The graph shows the dependence of the Q factor on the applied strain for devices with two different widths in the supporting ribbon. Panel **a** is adapted with permission from REF. 202, Elsevier. Panel **b** is adapted with permission from REF. 74, AAAS, and REF. 93, National Academy of Sciences. Panel **c** is adapted with permission from REF. 74, AAAS. Panel **d** is adapted with permission from REF. 75, AAAS.

Conclusion and outlook

Widespread emerging and envisioned applications of 3D micro- and nanostructures — from electronics and photonics, to energy storage and biomedicine — provide strong motivation for the development of new patterning concepts and advanced materials that create designer properties in metamaterials, and engineering design options beyond those of traditional planar systems. Recent progress has established a broad range of

techniques with impressive capabilities in forming 3D architectures, in which critical feature sizes can be as small as tens of nanometres or less, and the thicknesses and overall spatial extents can reach centimetres or more. Although the various available methods outlined in this article each offer powerful features, none is without limitations — some in accessible materials, others in realizable geometries and others in throughput and/or feature sizes. For example, TPL and nozzle-based printing

techniques offer remarkably high levels of control over 3D geometries, but further advances are needed to allow for rapid processing and use with high-performance materials¹⁴⁸. Assembly methods inspired by origami and kirigami concepts can operate at high speed, and systematic rules now exist in lattice kirigami methods^{203,204} and origami algorithms²⁰⁵ for folding flat plates into complex targeted 3D configurations. Nevertheless, schemes that avoid requirements for manual intervention, particularly at the micro- and nanoscale, are needed, as are approaches for use with high performance, active materials and advanced planar technologies. Mechanically guided assembly methods do not have such limitations, but the development of design rules for mapping desired 3D structures onto 2D precursors is in its infancy. The ability to combine these various methods together in an integrated approach might facilitate progress towards the ultimate goal of establishing methods that allow for rapid formation of arbitrary 3D architectures in any heterogeneous collection of constituent materials.

Of course, opportunities also exist in the exploration of fundamentally different types of approaches.

Materials science will remain at the core of these activities, but in ways that integrate expertise from the fields of electrical engineering, mechanical engineering, chemical engineering, cell biology, biomedical engineering and others. The foundational research encompasses many topics of fundamental interest in materials processing and heterogeneous integration; buckling, thin-film mechanics and nanomechanics; optics and electromagnetics; polymer science and physics; and adhesion and interface science. The technology pull associated with applications that can benefit from or are enabled by 3D geometries will continue to serve as a strong motivation for further research in this area. Even now, impressive progress outlined in this Review suggests that the question of how to build 3D structures will increasingly shift to what kinds of unique properties in metamaterials and applications in device technologies will follow from the enabled 3D geometries.

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